



basic education

Department:
Basic Education
REPUBLIC OF SOUTH AFRICA

NATIONAL SENIOR CERTIFICATE

GRADE 12

TECHNICAL MATHEMATICS P1

EXEMPLAR 2025

MARKS: 150

TIME: 3 hours

**This question paper consists of 11 pages, a 2-page information sheet and
a 21-page SPECIAL ANSWER BOOK.**

INSTRUCTIONS AND INFORMATION

Read the following instructions carefully before answering the questions.

1. This question paper consists of NINE questions.
2. Answer ALL the questions in the SPECIAL ANSWER BOOK provided.
3. Number the answers correctly according to the numbering system used in this question paper.
4. Clearly show ALL calculations, diagrams, graphs, etc. that you have used in determining your answers.
5. Answers only will NOT necessarily be awarded full marks.
6. You may use an approved scientific calculator (non-programmable and non-graphical), unless stated otherwise.
7. If necessary, round off answers to TWO decimal places, unless stated otherwise.
8. Diagrams are NOT necessarily drawn to scale.
9. An information sheet with formulae is included at the end of the question paper.
10. Write neatly and legibly.

QUESTION 11.1 Solve for x :

1.1.1 $x(2x + 7) = 0$ (2)

1.1.2 $3x^2 + x = 6 + 5x$ (correct to TWO decimal places) (4)

1.1.3 $x^2 + 3x - 10 \leq 0$ (3)

1.2 Solve for x and y if:

$y - x = 2$ and $x^2 + y^2 = 20$ (6)

1.3 The formula used to determine CR (compression ratio) when combustion and swept volumes are given is:

$$CR = \frac{CV + SV}{SV}$$

Where:

 CR = compression ratio CV = combustion volume (cm^3) SV = swept volume (cm^3)1.3.1 Make CV the subject of the formula. (2)1.3.2 Hence, calculate the numerical value of CV if $SV = 48 \text{ cm}^3$ and the compression ratio is equal to 9,5 : 1. (2)1.4 Express 1110_2 as a decimal number. (1)1.5 Evaluate $1110_2 \times 35$ and leave your answer as a binary number. (2)
[22]

QUESTION 2

2.1 Given: $x = \frac{-2 \pm \sqrt{1-7p}}{3-p}$. Determine the numerical value(s) of p if x is:

2.1.1 Undefined (1)

2.1.2 Non-real (2)

2.2 Determine the numerical value(s) of t for which the equation $3(x+1) = x^2 + t$ will have real roots. (4)
[7]

QUESTION 3

3.1 Simplify the following, **showing ALL calculations**, where applicable:

3.1.1 $27^{\frac{2}{3}}$ (1)

3.1.2 $(1 + \sqrt{3})^2 - \sqrt{12}$ (3)

3.1.3 $\log_p p$ (1)

3.1.4 $\log_3 81 - \log_2 \sin 30^\circ - \log_5 \sqrt{5}$ (4)

3.2 Solve for x : $5^{x+2} - 5^x = \frac{24}{5}$ (3)

3.3 Given the complex number: $z_1 = \frac{1}{2} \times z_2$ where $z_2 = -2i + 2$

3.3.1 Express z_1 in the form $a + bi$. (1)

3.3.2 Write down $\bar{z}_1$ (conjugate of z_1). (1)

3.3.3 Represent $\bar{z}_1$ (conjugate of z_1) as an Argand diagram on the complex plane provided in the SPECIAL ANSWER BOOK. (3)

3.3.4 Express z_1 in the form $r \operatorname{cis} \theta$, (θ in degrees). (5)
[22]

QUESTION 4

4.1 Given functions f and h defined by $f(x) = 3^x - 1$ and $h(x) = \sqrt{25 - x^2}$

4.1.1 Write down the equation of the asymptote of f . (1)

4.1.2 Write down the domain of h . (2)

4.1.3 Determine the x -intercept of f . (2)

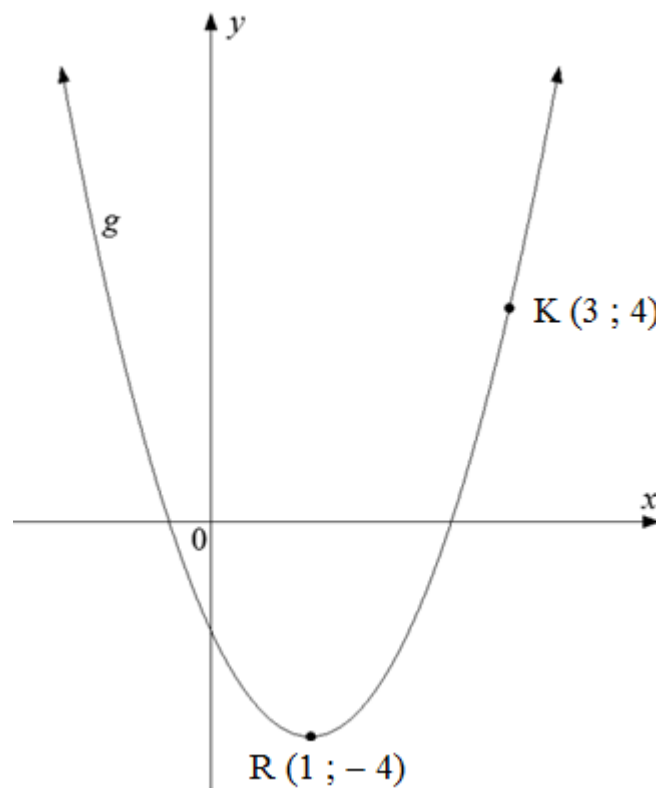
4.1.4 Determine the y -intercept of f . (2)

4.1.5 Draw sketch graphs of f and h on the same set of axes provided in the SPECIAL ANSWER BOOK. Clearly indicate ALL the intercepts with the axes and the asymptote. (5)

4.1.6 Hence, use your graph to determine the values of x for which $f(x) \times h(x) \leq 0$ (2)

4.2 The graph below represents function g defined by $g(x) = a(x - p)^2 + q$

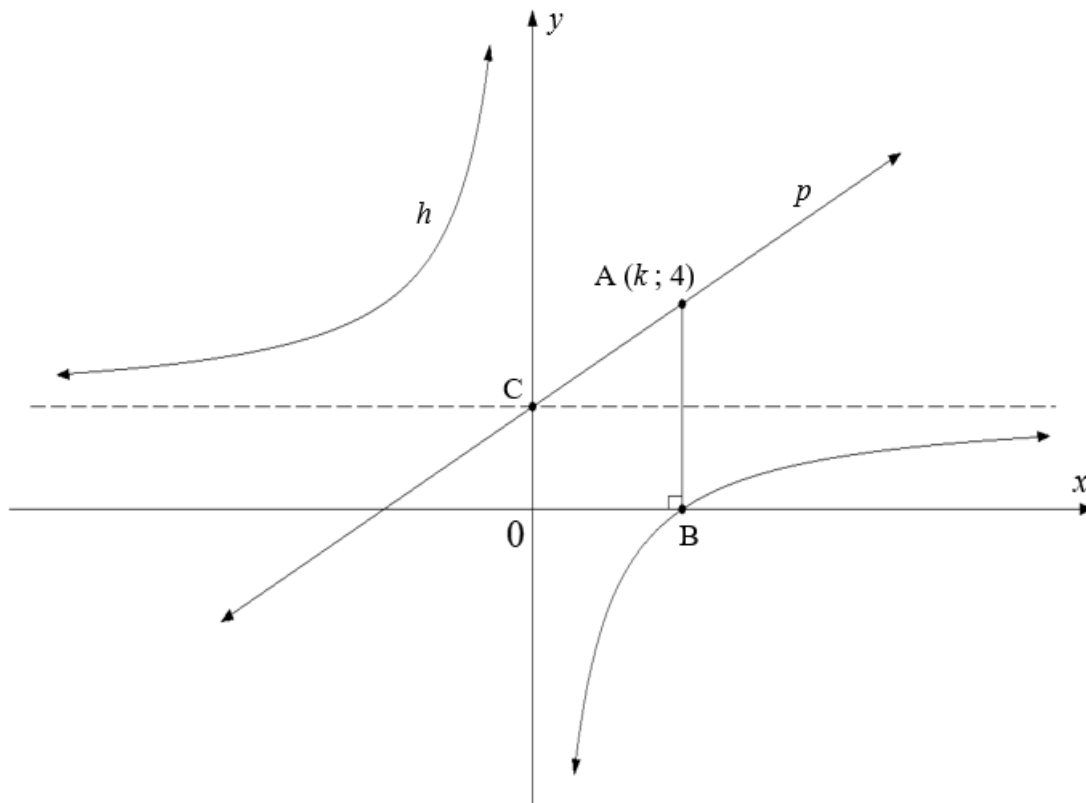
$R(1; -4)$ is the turning point of g and $K(3; 4)$ is a point on g .



Determine the equation of g in the form $g(x) = ax^2 + bx + c$ (4)

- 4.3 The graphs below represent functions h and p defined by $h(x) = \frac{a}{x} + q$ and $p(x) = x + 2$.

- $A(k; 4)$ is a point on p and B is the x -intercept of h .
- The asymptote of h passes through C , the y -intercept of p .
- AB is perpendicular to the x -axis.



- 4.3.1 Write down the equations of the asymptotes of h . (2)
- 4.3.2 Determine the numerical value of k . (2)
- 4.3.3 Hence, write down the x -coordinate of B . (1)
- 4.3.4 Hence, determine the defining equation of h . (2)
- [25]

QUESTION 5

- 5.1 The annual effective interest rate charged by a financial institution is 9,1%. Calculate the nominal interest rate charged per annum if it is compounded quarterly. (4)
- 5.2 A town's population increased from 50 000 at a compound rate of 3% per annum over a five-year period. Determine the population of the town at the end of five years. (3)
- 5.3 In 2018, engineering equipment costed R260 000.
- 5.3.1 If the equipment bought in 2018 depreciated to 25% of its original value, calculate the current value of the equipment. (1)
- 5.3.2 The equipment depreciated at a rate of 14% per annum using the reducing-balance method. Determine how long (to the nearest year) it took for the equipment to depreciate to the value calculated in QUESTION 5.3.1. (4)
- 5.4 An amount of R20 000 is invested into an account that offers an interest rate of 10% per annum, compounded monthly.
- At the end of 18 months, the interest rate changed to 8% per annum, compounded quarterly.
 - The interest rate then remained unchanged for the remaining years.
 - An amount of R3 000 was withdrawn from the account at the end of the 3rd year.
- Determine the amount of money in the investment account at the end of the 4th year. (5)

[17]

QUESTION 6

6.1 Given: $f(x) = 9x - 6$

Determine $f'(x)$ using FIRST PRINCIPLES. (5)

6.2 Determine $f'(x)$ if $f(x) = 11\pi^2$ (1)

6.3 Given: $y = x \left(3 + \frac{3}{x^5} \right)$

6.3.1 Simplify y . (2)6.3.2 Hence, determine $\frac{dy}{dx}$. (2)

6.4 Given: $D_x \left[\sqrt[5]{x^8} - 5x^{12} \right]$

6.4.1 Express $\sqrt[5]{x^8}$ in exponential form. (1)6.4.2 Hence, determine $D_x \left[\sqrt[5]{x^8} - 5x^{12} \right]$. (2)

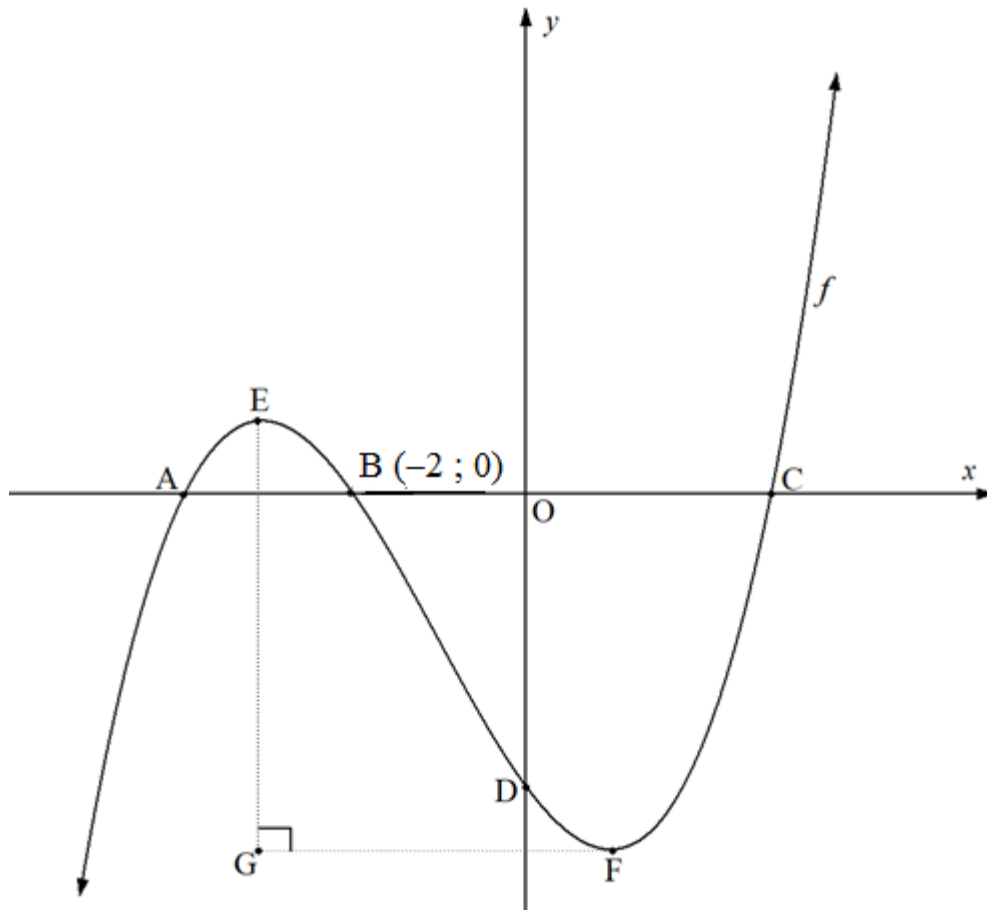
6.5 Given: $g(x) = -x^3 + 6x^2$

6.5.1 Determine $g'(x)$. (2)6.5.2 Hence, determine the gradient of the tangent to g at $x = -2$ (2)6.5.3 Determine the coordinates of a point of contact of another tangent to the curve that has the same gradient as the tangent at $x = -2$ (4)
[21]

QUESTION 7

The graph of function f , defined by $f(x) = x^3 + x^2 - 32x - 60$, is drawn below.

- Points A, B(-2 ; 0) and C are the x -intercepts and point D is the y -intercept of f .
- E and F are the turning points of f and $\hat{E}GF = 90^\circ$.



- 7.1 Write down the length of OD. (1)
- 7.2 Determine the coordinates of points A and C. (4)
- 7.3 Determine the coordinates of point G. (6)
- 7.4 Use the graph to determine the values of x for which:
- 7.4.1 $f(x) \geq 0$ if $x < 0$ (2)
- 7.4.2 f is decreasing (2)

[15]

QUESTION 8

A company manufactures x bottle caps weekly and makes a profit of P rands. The relationship between the profit and the number of bottle caps produced weekly is given by the following formula:

$$P(x) = -20x^3 + 6\,000x - 10\,000$$

Determine:

- 8.1 The loss for the company if it is closed for a week (1)
- 8.2 $P'(x)$ (1)
- 8.3 The maximum weekly profit that the company can make (5)
- [7]**

QUESTION 9

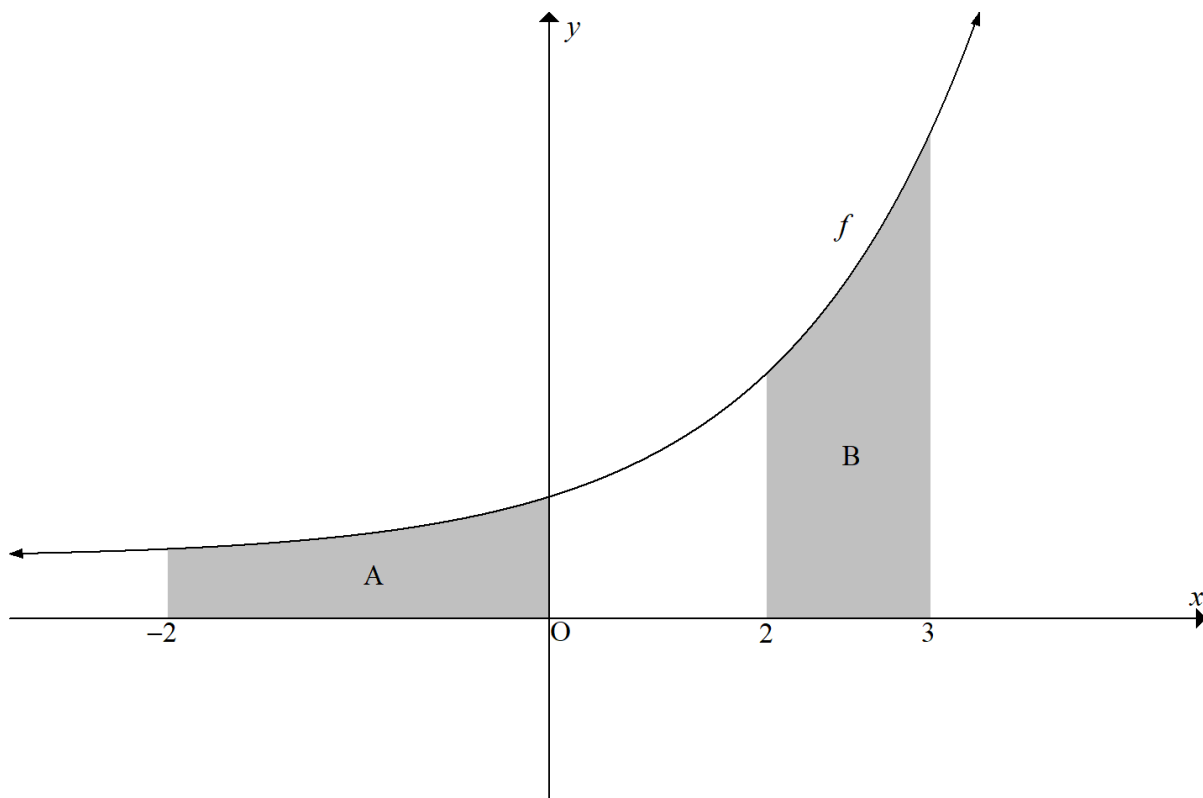
9.1 Determine the following integrals:

9.1.1 $\int -\frac{6}{x} dx$ (2)

9.1.2 $\int (3x - 4)(x + 2) dx$ (4)

9.2 The sketch below shows function f defined by $f(x) = 2^x$

- A represents the shaded area bounded by the graph of f , the x -axis and the ordinates $x = -2$ and $x = 0$
- B represents the shaded area bounded by the graph of f , the x -axis and the ordinates $x = 2$ and $x = 3$



9.2.1 Determine: $\int 2^x dx$ (1)

9.2.2 A learner claims that area B is equal to 4 times that of area A.

Verify, showing ALL calculations, whether the learner's claim is VALID.

(7)
[14]

TOTAL: 150

INFORMATION SHEET: TECHNICAL MATHEMATICS

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = -\frac{b}{2a}$$

$$y = \frac{4ac - b^2}{4a}$$

$$a^x = b \Leftrightarrow x = \log_a b, \quad a > 0, a \neq 1 \text{ and } b > 0$$

$$A = P(1 + ni)$$

$$A = P(1 - ni)$$

$$A = P(1 + i)^n$$

$$A = P(1 - i)^n$$

$$i_{eff} = \left(1 + \frac{i}{m}\right)^m - 1$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$\int k x^n dx = k \cdot \frac{x^{n+1}}{n+1} + C, \quad n \neq -1$$

$$\int \frac{k}{x} dx = k \cdot \ln x + C, \quad x > 0$$

$$\int k a^{nx} dx = k \cdot \frac{a^{nx}}{n \ln a} + C, \quad a > 0$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$M\left(\frac{x_2 + x_1}{2}; \frac{y_2 + y_1}{2}\right)$$

$$y = mx + c$$

$$y - y_1 = m(x - x_1)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$\tan \theta = m$$

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

$$\text{In } \triangle ABC: \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cdot \cos A$$

$$\text{Area of } \triangle ABC = \frac{1}{2} ab \cdot \sin C$$

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$1 + \tan^2 \theta = \sec^2 \theta$$

$$1 + \cot^2 \theta = \operatorname{cosec}^2 \theta$$

$$\pi \text{ rad} = 180^\circ$$

$$\text{Angular velocity} = \omega = 2 \pi n \quad \text{where } n = \text{rotation frequency}$$

$$\text{Angular velocity} = \omega = 360^\circ n \quad \text{where } n = \text{rotation frequency}$$

$$\text{Circumferential velocity} = v = \pi D n \quad \text{where } D = \text{diameter and } n = \text{rotation frequency}$$

$$\text{Circumferential velocity} = v = \omega r \quad \text{where } \omega = \text{angular velocity and } r = \text{radius}$$

$$\text{Arc length} = s = r \theta \quad \text{where } r = \text{radius and } \theta = \text{central angle in radians}$$

$$\text{Area of a sector} = \frac{r s}{2} \quad \text{where } r = \text{radius, } s = \text{arc length}$$

$$\text{Area of a sector} = \frac{r^2 \theta}{2} \quad \text{where } r = \text{radius and } \theta = \text{central angle in radians}$$

$$4h^2 - 4dh + x^2 = 0 \quad \text{where } h = \text{height of segment, } d = \text{diameter of circle} \\ \text{and } x = \text{length of chord}$$

$$A_T = a(m_1 + m_2 + m_3 + \dots + m_n) \quad \text{where } a = \text{width of equal parts, } m_1 = \frac{o_1 + o_2}{2} \\ o_n = n^{\text{th}} \text{ ordinate and } n = \text{number of ordinates}$$

OR

$$A_T = a \left(\frac{o_1 + o_n}{2} + o_2 + o_3 + \dots + o_{n-1} \right) \quad \text{where } a = \text{width of equal parts, } o_n = n^{\text{th}} \text{ ordinate} \\ \text{and } n = \text{number of ordinates}$$