



**higher education
& training**

Department:
Higher Education and Training
REPUBLIC OF SOUTH AFRICA

NASIENRIGLYN

NATIONALE CERTIFIKAAT INGENIEURSWETENSKAP N4

30 JULIE 2018

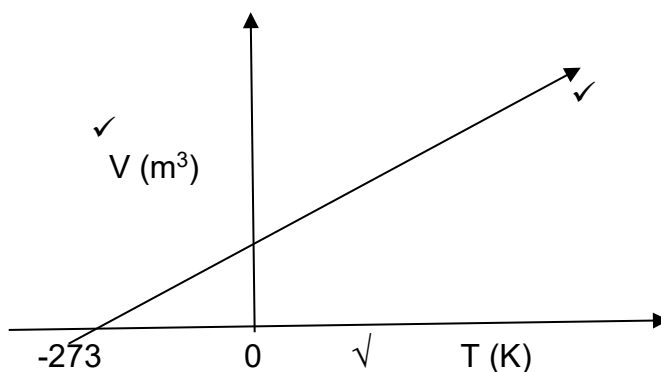
Hierdie nasienriglyn bestaan uit 14 bladsye.

VRAAG 1: ALGEMEEN

- 1.1 1.1.1 Resulterende snelheid: 'n enkele snelheid wat twee of meer snelhede voorstel wat op 'n punt inwerk, en wat dieselfde uitwerking het as hierdie snelhede.
- 1.1.2 Skuifkrag: die som van alle kragte na links of regs van 'n deel op 'n balk. (2 × 1) (2)
- 1.2 Newton se tweede bewegingswet: die tempo van momentum is direk eweredig aan en in dieselfde rigting as die krag wat uitgeoefen word. (2)
- 1.3 1.3.1 Dit is op die moment wat die veer elasties is.
OF
Dit is die moment waarop die veer tot sy oorspronklike vorm of grootte terugkeer wanneer die eksterne krag verwyder word. (1)
- 1.3.2 Elastisiteitsgrens: dit is die punt waar die veer nie na sy oorspronklike vorm of grootte terugkeer nie wanneer die eksterne krag voor permanente vervorming verwyder word. (2)
- 1.4 Suid 45 grade Oos OF S45° O (1)
- 1.5 1.5.1 Die hoeveelheid vloeistof wat van die pers geglip het
- 1.5.2 Hoe hoer die druk hoe joër die diepte van die volume. (2 × 1) (2)
- 1.6 Funksionele hidroulika: om hidrouliese energie te akkumuleer en dit met tussenposes te verbruik. (2)
- 1.7 Charles se gas-wet: by 'n konstante druk is die volume gas direk eweredig aan die temperatuur.✓

$$\frac{V_1}{T_1} = \frac{V_2}{T_2} \checkmark$$

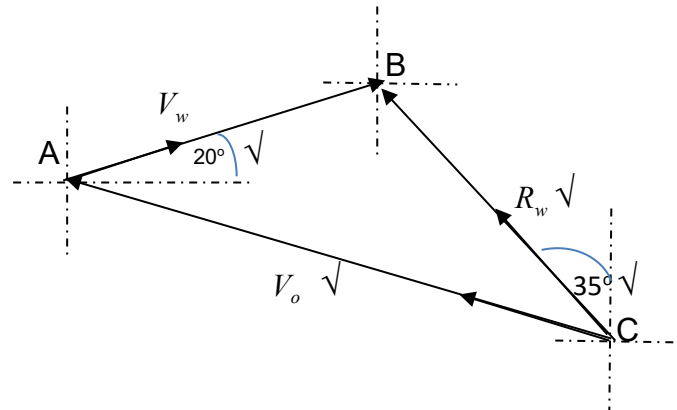
Snelheid – Temperatuur

(4)
[16]

VRAAG 2: KINEMATIKA

2.1 $V_o = 300 \text{ Km} / \text{h}$
 $V_w = 100 \text{ Km} / \text{h} \text{ E } 20^\circ \text{ N } V_w$
 $R_v = ? \quad \text{N } 35^\circ \text{ W}$

2.1 2.1.1



(2)

2.1.2

$$B = 35^\circ + 70^\circ$$

$$= 105^\circ$$

$$\frac{\sin C}{c} = \frac{\sin B}{b}$$

$$C = \sin^{-1} \left(\frac{c \sin B}{a} \right)$$

$$= \sin^{-1} \left(\frac{100 \sin 105}{300} \right)$$

$$= 18.782^\circ \checkmark$$

$$A = 180^\circ - (105^\circ + 18.782^\circ)$$

$$= 56.218^\circ \checkmark$$

$$a = \sqrt{b^2 + c^2 - 2bc \cos A}$$

$$= \sqrt{(300)^2 + (100)^2 - 2(300)(100) \cos 105}$$

$$= 339.896 \text{ km} / \text{h} \checkmark$$

$$\therefore R_v = 339.896 \text{ km} / \text{h} \text{ N } 35^\circ \text{ W} \checkmark$$

(3)

2.1.3 Die vlugrigting

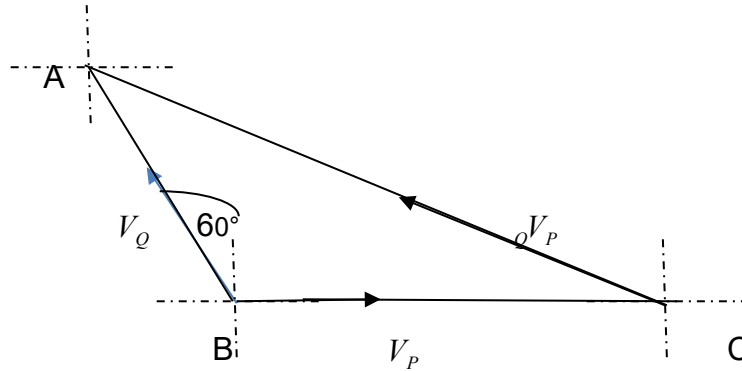
$$\beta = 90^\circ - (25^\circ + 18.782^\circ)$$

$$= 36.218^\circ$$

$$\text{Vlugrigting} = \text{W } 36.218^\circ \text{N} \checkmark \text{ OF } \text{N } 53.782^\circ \text{N} \checkmark$$

(1)

2.2 $V_P = 220 \text{ km/h } E$
 $V_Q = 220 \text{ km/h } W 30^\circ N$
 ${}_P V_Q = ?$



$$B = 60^\circ + 90^\circ$$

$$= 150^\circ$$

$$B = \sqrt{a^2 + c^2 - 2ac \cos B}$$

$$= \sqrt{(220)^2 + (220)^2 - 2(220)(220) \cos 150^\circ} \checkmark$$

$$= 425.007 \text{ km/h } \checkmark$$

$$\frac{\sin C}{c} = \frac{\sin B}{b}$$

$$C = \sin^{-1} \left(\frac{c \sin B}{a} \right)$$

$$= \sin^{-1} \left(\frac{220 \sin 150^\circ}{425.007} \right) \checkmark$$

$$= 15^\circ \quad \checkmark$$

$${}_Q V_P = 425.007 \text{ km/h } W 15^\circ N$$

(4)

2.3 $S_h = 210 \text{ m}$
 $V = 730 \text{ km/h}$
 $t = 3 \text{ s}$

$$S_h = t \cdot V \cdot \sin \theta \checkmark$$

$$\sin \theta = \frac{S_h}{t \cdot V}$$

$$\theta = \sin^{-1} \left(\frac{S_h}{t \cdot V} \right)$$

$$\theta = \sin^{-1} \left(\frac{210}{3(202.778)} \right) \checkmark$$

$$= 20.194^\circ \checkmark$$

(3)
[13]

VRAAG 3: HOEKBEWEGING

- 3.1 B
3.2 C
3.3 B
3.4 D

(4 × 2) [8]

VRAAG 4: DINAMIKA

- 4.1 4.1.1 $m = 780\text{kg}$
 $\text{slope} = 7\%$
 $S = 25\text{m}$

$$\theta = \tan^{-1}\left(\frac{7}{100}\right)$$

$$= 4.004^\circ \checkmark$$

$$E_p = mgh$$

$$= 780\text{kg}(9.8\text{m/s}^2)25\text{Sin}(4.004)$$

$$= 13343.771\text{J} \checkmark$$

$$E_{k(\text{bottom})} = E_{p(\text{top})} \checkmark$$

$$= 13343.771\text{J}$$

$$V = \sqrt{\frac{4(13343.771)}{789}} \checkmark$$

$$= 8.225\text{m/s} \checkmark$$

(3)

4.1.2

$$V^2 = u^2 + 2aS$$

$$a = \frac{0^2 - (8.225\text{m/s})^2}{2(35)} \checkmark$$

$$= -0.966\text{m/s}^2 \checkmark$$

(2)

4.1.3 $E_k = 0\text{m/s} \checkmark$

(1)

4.2 4.2.1 $m = 1.8 \text{ ton}$
 $\text{plane} = \text{horizontal}$
 $S = 35 \text{ m}$
 $f_u = 110 \text{ N / ton}$
 $U = 20 \text{ m/s}$
 $V = 0 \text{ m/s} \checkmark$

$$V^2 = u^2 + 2aS$$

$$a = \frac{0^2 - (20 \text{ m/s})^2}{2(35)} \checkmark$$

$$= -5.714 \text{ m/s}^2 \checkmark$$

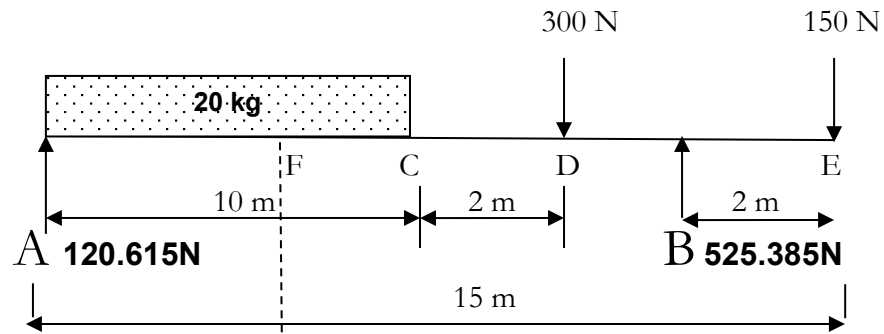
4.2.2 f_{brake}
 $f_{\text{app}} = -(f_B + f_u) \checkmark$
 $f_{\text{app}} = 1800 \text{ kg}(-5.714 \text{ m/s}^2)$
 $= -10285.714 \text{ N} \checkmark$
 $f_u = 1.8 \text{ ton}(110 \text{ N / ton})$
 $= 198 \text{ N} \checkmark$
 $f_B = -f_{\text{app}} - f_u$
 $= -(-10285.714 \text{ N}) - 198 \text{ N} \checkmark$
 $= 10087.714 \text{ N} \checkmark$

(2 × 3) (6)
 [12]

VRAAG 5: STATIKA

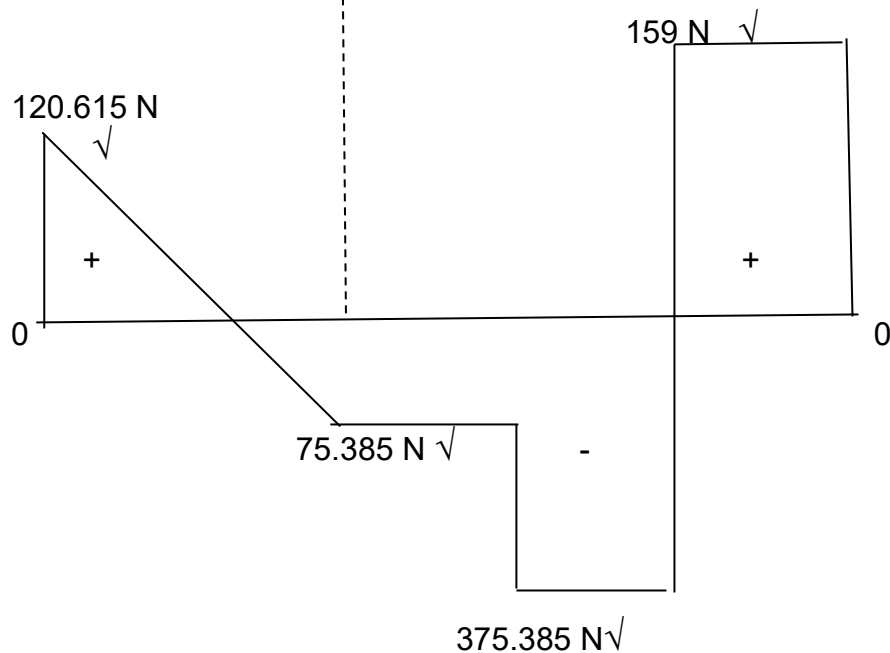
5.1 5.1.1 $\text{spring} = (20 \text{ Kg})(98 \text{ m/s}^2)$
 $f_{\text{spring}} = \frac{(20 \text{ Kg})(98 \text{ m/s}^2)}{10 \text{ m}}$
 $= 19,6 \text{ N / m}$
 $\Delta \cong A$
 $\sum F_{\perp} \cdot S(ac) = \sum F_{\perp} \cdot (c)$
 $B(13 \text{ m}) = 196 \text{ N}(5 \text{ m}) + 300 \text{ N}(12 \text{ m}) + 150 \text{ N}(15 \text{ m})$
 $B \Rightarrow \frac{6830 \text{ Nm}}{13 \text{ m}} = 525,385 \text{ N} \checkmark$
 $\Delta \cong B$
 $\sum F_{\perp} \cdot S(ac) = \sum F_{\perp} \cdot (c)$
 $196 \text{ N}(8 \text{ m}) + 300 \text{ N}(1 \text{ m}) = 150 \text{ N}(2 \text{ m}) + A(13 \text{ m})$
 $A \Rightarrow \frac{1568 \text{ Nm}}{13 \text{ m}} = 120,615 \text{ N} \checkmark$

(2)



Bereken:

5.1.2



(2)

5.1.3 $BM_A \rightarrow (120.615 \text{ N}) \cdot (0 \text{ m}) = 0$

$$BM_C \rightarrow (120.615 \text{ N}) \cdot (10 \text{ m}) - (196 \text{ N}) \cdot (5 \text{ m}) = 226.15 \text{ Nm} \checkmark$$

$$BM_D \rightarrow (120.615 \text{ N}) \cdot (12 \text{ m}) - (196 \text{ N}) \cdot (7 \text{ m}) = 75.38 \text{ Nm} \checkmark$$

$$BM_B \rightarrow (120.615 \text{ N}) \cdot (13 \text{ m}) - (196 \text{ N}) \cdot (8 \text{ m}) - 300 \text{ N} \cdot (1 \text{ m}) = -300.005 \text{ Nm} \checkmark$$

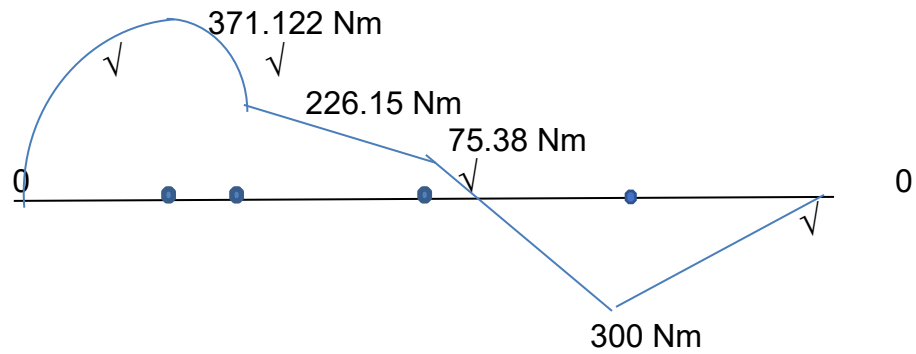
$$BM_E \rightarrow (120.615 \text{ N}) \cdot (15 \text{ m}) - (196 \text{ N}) \cdot (10 \text{ m}) - (300 \text{ N}) \cdot (3 \text{ m}) - (130 \text{ N}) \cdot (0 \text{ m}) = 0$$

$$\begin{aligned} \sum f_s &= 0 \\ 120.615 \text{ N} - (19.6 \text{ N/m}) \cdot x &= 0 \\ x &= \frac{-120.615 \text{ N}}{-19.6 \text{ N/m}} \\ &= 6.154 \text{ m} \checkmark \end{aligned}$$

$$\begin{aligned} BM_F &\rightarrow (120.615 \text{ N}) \cdot (6.154 \text{ m}) - \\ &\quad (19.6 \text{ N}) \cdot (6.154 \text{ m}) \cdot (0.5) \cdot (2.333 \text{ m}) \\ &= 371.122 \text{ Nm} \checkmark \end{aligned}$$

(5)

5.1.4



(2)

5.2

Vorm	V (mm ³)	G (mm)	VG (mm ⁴)
Silinder A	$V_A = \frac{\pi D^2}{4} H$ $= \frac{\pi 50^2}{4} 20$ $= 39269.908 \sqrt{}$	$G = \frac{H}{2}$ $= \frac{20}{2}$ $= 10 \sqrt{}$	$39269.908(10)$ $= 392699.08 \sqrt{}$
Silinder B	$V_B = \frac{\pi d^2}{4} h$ $= \frac{\pi 30^2}{4} 80$ $= 56548.668 \sqrt{}$	$G = H + \frac{h}{2}$ $= 20 + \frac{80}{2}$ $= 60 \sqrt{}$	$56548.668(60)$ $= 3392920.066 \sqrt{}$
	$\sum v. = 39269.908 + 56548.668$ $= 95818.576 \sqrt{}$	$y = \frac{\sum v.G}{\sum V}$ $= 39.508 \text{ mm} \sqrt{}$	$\sum v.G = 392699.08 + 3392920.$ $= 3785619.146 \sqrt{}$

(4)
[15]

VRAAG 6: HIDROULIKA

6.1 6.1.1 d = 90 mm D = 180 mm

Sl = 480 mm

MA = 18

$\eta = 85\%$

f_h , m=4.2Mg $\eta = 96\%$

$$\frac{W_R}{f_p} = \frac{D^2}{d^2} \quad \text{and} \quad MA = \frac{f_p}{f_h} \cdot \frac{100}{\eta}$$

$$W_R = 4.2 \times 10^3 \text{ kg}(9.8 \text{ m/s}^2) \\ = 41160 \text{ N} \checkmark$$

$$f_p = \frac{d^2 W_R}{D^2}$$

$$f_p = \frac{(0.09 \text{ m})^2 41160 \text{ N}}{(0.18 \text{ m})^2} \checkmark \\ = 10290 \text{ N} \checkmark$$

$$f_h = \frac{f_p}{MA} \cdot \frac{100}{\eta} \\ = \frac{10290 \text{ N}}{18} \cdot \frac{100}{96} \checkmark \\ = 595.486 \text{ N} \checkmark$$

(5)

6.1.2 n, m = 4.2 Mg SL = 520 mm $\eta = 96\%$

$$V_a = \frac{\pi \cdot D^2 S_L \cdot}{4} \\ = \frac{\pi (0.180 \text{ m})^2 (0.520 \text{ m})}{4}$$

$$= 0.0132324 \text{ m}^3 \checkmark$$

$$V_s = V_a \cdot \frac{100}{\eta} \\ = 0.0132324 \text{ m}^3 \frac{100}{96} \\ = 0.01378374 \text{ m}^3$$

$$\frac{\pi \cdot d^2 \cdot sl \cdot n}{4} = 0.01378374 \text{ m}^3$$

$$n = 4.513 \approx 4.5 \checkmark$$

(3)

6.2 6.2.1 $N = 120 \text{ r/min}$
 $d = 150 \text{ mm}$
 $S_l = 250 \text{ mm}$
 $C = 2$

V_a (Werklike volume in l/s), $S_L = 300 \text{ mm}$

$$V_s = \frac{\pi \cdot d^2 \cdot s \cdot l \cdot n \cdot C}{4} \cdot \frac{N}{60}$$

$$= \frac{\pi \cdot (0,150 \text{ m})^2 \cdot 0,25 \text{ m} \cdot 1 \cdot (2)}{4} \cdot \frac{120 \text{ r/min}}{60} \checkmark$$

$$= 0,0176715 \text{ m}^3 / \text{s} \checkmark$$

$$V_a = V_s \cdot \frac{\eta}{100}$$

$$= 0,0176715 \text{ m}^3 / \text{s} \cdot \frac{100}{100} \checkmark$$

$$= 0,0176715 \text{ m}^3 / \text{s} (1000 \text{ l} / \text{m}^3)$$

$$= 17,671 \text{ l} / \text{s} \checkmark$$

(4)

6.2.2 $Slip\% = \frac{V_s - V_a}{V_s} \cdot 100$

$$= \frac{17,671 \text{ l/s} - 16,789 \text{ l/s}}{17,671 \text{ l/s}} \cdot 100 \checkmark$$

$$= 5,037\% \quad \checkmark$$

$$\approx 5\%$$

(2)

[14]

VRAAG 7: SPANNING, VERVORMING EN YOUNG SE ELASTISITEITSMODULUS

$$7.1 \quad D_{ext} : d_{int}$$

$$3:1$$

$$F = 620kN$$

$$\Delta l = 0.771mm$$

$$E = 209GPa$$

$$l = 3m$$

$$\Delta l = 0.771mm$$

$$D_{ext} = ?$$

$$d_{int} = ?$$

$$\epsilon = \frac{\Delta l}{l}$$

$$= \frac{0.771mm}{3000mm}$$

$$= 0.000257 \quad \checkmark$$

$$E = \frac{\delta}{\epsilon}$$

$$\delta = E \cdot \epsilon$$

$$= 209 \times 10^9 Pa \cdot (0.000257)$$

$$= 53713000Pa \quad \checkmark$$

$$\delta = \frac{F}{a}$$

$$\therefore a = \frac{F}{\delta}$$

$$= \frac{620000N}{53713000Pa}$$

$$= 0.0115428m^2 \quad \checkmark$$

$$a = \frac{\pi}{4}(D_{ext}^2 - d_{int}^2)$$

$$= \frac{\pi}{4}((3d_{int})^2 - d_{int}^2) \quad \checkmark$$

$$= \frac{\pi}{4}8d_{int}^2$$

$$= 6.283185d_{int}^2$$

$$d_{int} = \sqrt{\frac{0.0115427m^2}{6.283185N}}$$

$$= 0.04286m \quad \checkmark \quad \text{or } (42.861 \text{ mm})$$

(6)

$$D_{ext} = 0.128583m \quad \checkmark \quad \text{or } (128.583 \text{ mm})$$

7.2 7.2.1 $F = 38kN$
 $a = 8000mm^2$
 $l = 3m$
 $\Delta l = 0.51mm$
 $a = \frac{800mm^2(1m^2)}{1 \times 10^6 mm^2}$
 $a = 0.008m^2 \checkmark$
 $\delta = \frac{F}{a}$
 $= \frac{38000N}{0.008m^2}$
 $= 4750000Pa \checkmark$

7.2.2 vervorming
 $\varepsilon = \frac{\Delta l}{l}$
 $= \frac{0.51mm}{4000mm} \checkmark$
 $= 1.275 \times 10^{-4} \checkmark$

7.2.3 E
 $E = \frac{\delta}{\varepsilon}$
 $= \frac{4750000Pa}{1.275 \times 10^{-4}} \checkmark$
 $= 3.7255 \times 10^{10} Pa$
 $= 37.255 \times GPa \checkmark$

(3 × 2) (6)
[12]

VRAAG 8: HITTE

$$\begin{aligned}
 8.1 \quad V &= 0.77m^3 \\
 \gamma &= 17 \times 10^{-7} / K \\
 \Delta T &= 233K \\
 \Delta V &= V_o \cdot \gamma \cdot \Delta T \\
 \Delta V &= 0.77m^3 \cdot 17 \times 10^{-7} / K \cdot (233K) \\
 &= 0.00304997m^3 \checkmark \\
 \Delta V &= V_2 - V_o \\
 V_2 &= \Delta V + V_o \\
 &= 0.00304997m^3 + 0.77m^3 \\
 &= 0.773m^3 \checkmark
 \end{aligned} \tag{3}$$

8.2 8.2.1 A

$$\begin{aligned}
 V_A &= 2m^3 & m_B &= 6kg \\
 t_A &= 25^\circ C & V_B &= ? \\
 P_A &= 580kPa & t_A &= 35^\circ C \\
 & & P_B &= 580kPa \\
 & & R &= 287J/kg.K \\
 & & t_{eqil} &= 20^\circ C \\
 T_A &= 298K \checkmark & T_{equi} &= 293K & T_B &= 308K \checkmark \\
 V_B &= ? \\
 P_B V_B &= m_B R T_B \\
 V_B &= \frac{m_B R T_B}{P_B} \\
 &= \frac{6kg(287J/kg.K).(308K)}{580000Pa} \checkmark \\
 &= 0.914m^3
 \end{aligned} \tag{3}$$

8.2.2

$$P_{equi} = ?$$

$$P_{equi} V_{equi} = m_{equi} R T_{equi}$$

$$V_{equi} = V_A + V_B$$

$$= 2m^3 + 0.914m^3$$

$$= 2.914m^3 \checkmark$$

$$P_A V_A = m_A R T_A$$

$$m_A = \frac{P_A V_A}{R T_A}$$

$$= \frac{580000 Pa (2m^3)}{(287 J / kg.K) (298 K)} \checkmark$$

$$= 13.563 kg \checkmark$$

$$P_{equi} \Rightarrow \frac{m_{equi} R T_{equi}}{V_{equi}} = \frac{13.563 (287) (293 K)}{2.914} \checkmark$$

$$P_{equi} = 391.395 kPa \checkmark$$

(4)
[10]**TOTAAL: 100**